# A model for right-handed neutrino magnetic moments

Alberto Aparici", Arcadi Santamaria", José Wudka-

<sup>a</sup>Departament de Física Teòrica, Universitat de València and IFIC, Universitat de Valèn
ia-CSIC Dr. Moliner 50, E-46100 Burjassot (Valèn
ia), Spain  ${}^b$ Department of Physics and Astronomy, University of California, Riverside CA 92521-0413, USA

# ${\bf Abstract}$

A simple extension of the Standard Model providing Majorana magnetic moments to right-handed neutrinos is presented. The model contains, in addition to the Standard Model parti
les and right-handed neutrinos, just a singly charged scalar and a vector-like charged fermion. The phenomenology of the model is analysed and its impli
ations in osmology, astrophysi
s and lepton flavour violating processes are extracted. If light enough, the charged particles responsible for the right-handed neutrino magnetic moments could opiously be produ
ed at the LHC.

 $Key words:$  Neutrinos, magnetic moments, effective Lagrangian, LHC PACS: 14.60.St, 13.35.Hb, 13.15.+g, 13.66.Hk

#### 1. Introdu
tion

In ref. 1 we studied the most general effective Lagrangian built with the Standard Model (SM) fields plus right-handed neutrinos up to operators of dimension five. We found this Lagrangian contains only three nonrenormalizable operators, one of them being the well known Weinberg operator  $[2]$  $[2]$ which only involves the SM lepton doublets and the Higgs doublet. The other two ontain an intera
tion of right-handed neutrinos with the SM Higgs doublet and a Majorana electroweak moment for the right-handed neutrinos. This last operator is particularly interesting and can have a variety of phenomenological consequences in cosmology, astrophysics and at colliders [1]. Of ourse, it is interesting to have expli
it models in whi
h these nonrenormalizable interactions arise naturally because one can use them to check the general features of the effective Lagrangian approach and extend them

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outside the realm of validity of the effective field theory. This is especially important if the parti
les responsible for the new intera
tions are light enough as to be produ
ed at the next generation of olliders.

Here we present a very simple model whi
h gives rise to right-handed neutrino electroweak moments; it includes, in addition to the SM fields and the right-handed neutrinos, a harged s
alar singlet and a harged singlet ve
tor-like fermion. We obtain the tree level and one-loop ontributions to the dimension five effective Lagrangian, and in particular we compute the ontribution to the right-handed neutrino ele
troweak moments. We perform a thorough phenomenological analysis of the model, paying special attention to the ase in whi
h the new harged parti
les are light enough to be pro-duced at the Large Hadron Collider (LHC). Thus, in section [2](#page-1-0) we define the model and ompute the one-loop ontribution to the ele
troweak moment of right-handed neutrinos. The simplest version of the model, in whi
h several ouplings are set to zero by using global symmetries, ontains stable harged massive parti
les (CHAMPs) whi
h are strongly disfavoured from osmological and astrophysical considerations. To avoid such problems we extend minimally the model by allowing a soft breaking of the symmetries, whi
h is enough to indu
e CHAMP de
ays; su
h de
ays are studied in se
tion [2.3.](#page-6-0) The model also induces some tree-level lepton flavour violating (LFV) processes like  $\mu \to 3e$  $\mu \to 3e$  $\mu \to 3e$  which are studied in section [2.4.](#page-8-0) In section 3 we discuss briefly the one-loop contributions of the model to the effective Higgs- $\nu_R$  op-erator. In section [4](#page-11-0) we compute the production cross section of the charged parti
les at the LHC and dis
uss their observability as a fun
tion of their masses. Finally, in section [5](#page-13-0) we present our conclusions.

## <span id="page-1-0"></span>2. The model

As discussed in ref. [1] the most general dimension five interactions among SM fields and three right-handed neutrinos can be written  $as<sup>1</sup>$  $as<sup>1</sup>$  $as<sup>1</sup>$ 

<span id="page-1-2"></span>
$$
\mathcal{L}_5 = \overline{\nu_R^c} \zeta \sigma^{\mu\nu} \nu_R B_{\mu\nu} + \left(\overline{\tilde{\ell}} \phi\right) \chi \left(\tilde{\phi}^\dagger \ell\right) - \left(\phi^\dagger \phi\right) \overline{\nu_R^c} \xi \nu_R + \text{h.c.} \tag{1}
$$

<span id="page-1-1"></span><sup>&</sup>lt;sup>1</sup>The reader should note a difference in notation respect to [1], where we used  $\nu'$  to denote the neutrino flavor eigenfields. As in the present work we are not going to discuss the diagonalisation of the neutrino mass matrices we will just use  $\nu$  to represent the flavor eigenfields.

where  $\ell = \binom{\nu_L}{e_L}$  $\genfrac{}{}{0pt}{}{\nu_L}{e_L}$  denotes the left-handed lepton isodoublet,  $e_R$  and  $\nu_R$  the corresponding right-handed isosinglets, and  $\phi$  the scalar isodoublet (family and gauge indi
es will be suppressed when no onfusion an arise). The harge conjugate fields are defined as  $e_R^c = C \bar{e}_R^T$ ,  $\nu_R^c = C \bar{\nu}_R^T$  and  $\tilde{\ell} = \epsilon C \bar{\ell}^T$ ,  $\tilde{\phi} = \epsilon \phi^*$ where  $\epsilon = i\sigma_2$  acts on the  $SU(2)$  indices. The hypercharges assignments are  $\phi : 1/2, \ell : -1/2, e_R : -1, \nu_R : 0$ . The  $SU(2)$  and  $U(1)$  gauge fields are denoted by  $W$  and  $B$  respectively (gluon and quarks fields will not be needed in the situations considered below). The couplings  $\chi$ ,  $\xi$ ,  $\zeta$  have dimension of inverse mass, whi
h is asso
iated with the s
ale of the heavy physi
s responsible for the corresponding operator.  $\chi$ , and  $\xi$  are complex symmetric  $3 \times 3$  matrices in flavour space, while  $\zeta$  is a complex antisymmetric matrix proportional to the right-handed neutrino ele
troweak moments.

The different terms in eq.  $(1)$  and their phenomenological consequences were discussed in  $|1|$ . Here we are more interested in models that could give rise to  $\zeta$ . This can only occur at the one-loop level and the models should ne
essarily involve either a s
alar-fermion pair with opposite (nonzero) hypercharges and having Yukawa couplings with both  $\nu_R$  and  $\nu_R^c$ , or a ve
tor-fermion pair with the same properties. Here we will onsider only the first (simpler) possibility. Thus we enlarge the SM by adding a negatively charged scalar singlet  $\omega$ ,  $Y(\omega) = -1$ , and one negatively charged vector-like fermion E (two chiralities and no generation indices) also with  $Y(E) = -1$ .

We can then write the Lagrangian as

$$
\mathcal{L} = \mathcal{L}_{\rm SM} + \mathcal{L}_{\rm NP} \;, \tag{2}
$$

where  $\mathcal{L}_{SM}$  is the SM Lagrangian while the new physics Lagrangian,  $\mathcal{L}_{NP}$ , collects all the terms containing any of the new particles, including among them the right-handed neutrinos. We write  $\mathcal{L}_{\text{SM}}$  as

$$
\mathcal{L}_{\rm SM} = i\overline{\ell} \mathcal{D} \ell + i\overline{e_R} \mathcal{D} e_R + (\overline{\ell} Y_e e_R \phi + \text{h.c.}) + \cdots \tag{3}
$$

with  $Y_e$  the Yukawa couplings of charged leptons which are completely general  $3 \times 3$  matrices in flavour space; the dots represent SM gauge boson, Higgs boson and quark kineti terms, quark Yukawa intera
tions and the SM Higgs potential. We divide the new physics contribution,  $\mathcal{L}_{NP}$ , in different terms:

$$
\mathcal{L}_{NP} = \mathcal{L}_K + \mathcal{L}_Y - V_{NP} + \mathcal{L}_{Extra}
$$
\n<sup>(4)</sup>

 $\mathcal{L}_K$  describes the kinetic terms of the new particles

$$
\mathcal{L}_K = D_{\mu}\omega^{\dagger}D^{\mu}\omega + i\overline{E}\mathcal{D}E - m_E\bar{E}E + i\bar{\nu}_R\partial\nu_R - \left(\frac{1}{2}\overline{\nu_R^c}M_R\nu_R + \text{h.c.}\right) \tag{5}
$$

with  $M_R$  the Majorana mass term of right-handed neutrinos, which is a complex symmetric matrix in flavour space.  $\mathcal{L}_Y$  contains the standard Yukawa intera
tions of right-handed neutrinos and the Yukawa ouplings of righthanded neutrinos with the particles needed to generate the electroweak moments:

$$
\mathcal{L}_Y = \overline{\ell} Y_\nu \nu_R \tilde{\phi} + \overline{\nu_R^c} h' E \omega^+ + \overline{\nu_R} h E \omega^+ + \text{h.c.}
$$
 (6)

 $Y_{\nu}$  is a general  $3 \times 3$  complex matrix and, if there is just one E, h and h' are vectors in generation space. The  $\omega$  contributions to the scalar potential are

$$
V_{NP} = m_{\omega}^2 |\omega|^2 + \lambda_{\omega} |\omega|^4 + 2\lambda_{\omega\phi} |\omega|^2 \phi^{\dagger} \phi , \qquad m_{\omega}^2 = m_{\omega}^2 + \lambda_{\omega\phi} v^2 \qquad (7)
$$

Where v is the vacuum expectation value of the Higgs doublet,  $\langle \phi^\dagger \phi \rangle = v^2/2$ , and the  $\lambda$ 's are quartic scalar couplings. We assume  $\lambda, \lambda_{\omega} > 0$  and  $\lambda \lambda_{\omega} > \lambda_{\omega \phi}^2$ to insure global (tree-level) stability, as well as  $m_{\omega}^2 > 0$  in order to preserve  $U(1)_{\text{em}}$ . It is important to remark that with only one Higgs doublet there cannot be trilinear couplings between the doublet and the singlet,  $\omega$ . Then, the potential has two independent  $U(1)$  symmetries, one for the singlet and one for the doublet.

In addition, the SM symmetries allow the following Yukawa couplings and mass terms

<span id="page-3-0"></span>
$$
\mathcal{L}_{Extra} = \bar{E}_L \kappa e_R + \bar{\ell} Y_E E_R \phi + \bar{\tilde{\ell}} f \ell \omega^+ + \bar{e}_R f' \nu_R^c \omega + \text{h.c.}
$$
 (8)

which can be set to zero by imposing a discrete symmetry which affects only the new parti
les

$$
E \to -E \,, \qquad \omega \to -\omega \tag{9}
$$

In this case all low-energy physics effects will be loop generated [\[3](#page-14-2)]. Notice that the resulting Lagrangian has a larger ontinuous symmetry

<span id="page-3-1"></span>
$$
E \to e^{i\alpha} E \,, \qquad \omega \to e^{i\alpha} \omega \tag{10}
$$

which is not anomalous, therefore there is a charge, carried only by  $E$  and  $\omega$  which is exactly conserved. In that case, the lightest of the E or  $\omega$  will



<span id="page-4-0"></span>Figure 1: Contributing diagrams to the right-handed neutrino electroweak moment.

be completely stable becoming a CHAMP, which could create serious problems in standard osmology s
enarios. However, su
h problems an easily be evaded by allowing some of the terms in eq. [\(8\)](#page-3-0). We will return to this issue after verifying that the model indeed generates a right-handed neutrino magneti moment.

# 2.1. The  $\nu_R$  magnetic moment

In the model considered we have two diagrams, depicted in figure [1,](#page-4-0) contributing to the  $\nu_R$  Majorana electroweak moment: a) loop with the B gauge boson attached to the  $E$  and b) loop with the  $B$  gauge boson attached to the scalar  $\omega$ .

For  $M_R \ll m_E, m_\omega$  we can neglect all external momenta and masses and the calculation of the diagrams simplifies considerably. The final result can be cast as a contribution to the effective magnetic moment operator in eq. [\(1\)](#page-1-2). We find

$$
\zeta_{ij} = \frac{g'f(r)}{(4\pi)^2 4m_E} \left( h_i' h_j^* - h_j' h_i^* \right) \tag{11}
$$

with  $r = (m_\omega/m_E)^2$ , g' the  $B_\mu$  gauge coupling and

<span id="page-4-1"></span>
$$
f(r) = \frac{1}{1-r} + \frac{r}{(1-r)^2} \log(r) \to \begin{cases} 1, & r \ll 1 \\ 1/2, & r = 1 \\ (\log(r) - 1)/r, & r \gg 1 \end{cases}
$$
 (12)

For an estimate we can take, for instance,  $m_{\omega} = m_E$ , and  $\left( h_i' h_j^* - h_j' h_i^* \right) =$ 0.5 while  $g' = \sqrt{\alpha 4\pi}/c_W \approx 0.35$ , then  $\zeta \approx 10^{-4}/m_E$  (for  $m_E \gg m_\omega$  there

will be a factor 2 enhancement and for  $m_E \ll m_\omega$  there will be a suppression by roughly a factor  $(m_E/m_\omega)^2$ ); these values are in agreement with the estimates obtained using effective field theory. In terms of  $\Lambda_{NP} \equiv 1/\zeta$  we have  $\Lambda_{NP} = 10^4 m_E$ . Present bounds from LEP and Tevatron give  $m_E \gtrsim 100 \,\text{GeV}$ , which imply  $\Lambda_{NP} \gtrsim 10^6 \,\text{GeV}$ . This can be compared with direct bounds that can be set on the right-handed neutrino electroweak moments derived in  $[1]$  $[1]$ . As expected, collider limits on E production are much more restrictive than collider limits derived from the induced electroweak moment interaction. After all, the ele
troweak moment intera
tion is generated at one loop. However, if the right-handed neutrinos are relatively light (below 10 MeV) bounds from transition magnetic moments coming from supernova cooling (which are  $\Lambda_{NP} \gtrsim 4 \times 10^6$  GeV) or red giant cooling (which are  $\Lambda_{NP} \gtrsim 4 \times 10^9$  GeV for  $m_N \lesssim 10 \,\text{keV}$  can be much stronger.

## 2.2. E or  $\omega$  as CHAMPs

The model as described so far contains only the couplings necessary to generate the right-handed neutrino Ma jorana ele
troweak moments. But it is clear that the trilinear vertices  $\bar{\nu}_R E \omega^\dagger$  and  $\bar{\nu}_R^c E \omega^\dagger$  alone cannot induce decays for both the E and the  $\omega$ . The lightest of the two will remain stable and could then accumulate in the galaxy clusters, appearing as electrically harged dark matter. The idea that dark matter ould be omposed mostly of charged massive particles was proposed in  $[4, 5]$  $[4, 5]$  $[4, 5]$  $[4, 5]$  and it is strongly constrained from very different arguments  $[6, 7, 8, 9, 10]$  $[6, 7, 8, 9, 10]$  $[6, 7, 8, 9, 10]$  $[6, 7, 8, 9, 10]$  $[6, 7, 8, 9, 10]$  $[6, 7, 8, 9, 10]$  $[6, 7, 8, 9, 10]$  $[6, 7, 8, 9, 10]$  $[6, 7, 8, 9, 10]$  $[6, 7, 8, 9, 10]$ . One might still consider the possibility of having massive stable E or  $\omega$  particles within the reach of the LHC, but with a cosmic abundance lower than the one required for dark matter. Unfortunately, su
h s
enario seems also to be ex
luded: if one assumes, as in [\[4](#page-14-3)], that the E's and  $\omega$ 's were produced in the early universe through the standard freeze-out mechanism  $|11|$ , the bounds from interstellar calorimetry [10] and terrestrial searches for super-heavy nuclei [\[7](#page-14-6), 8] completely close the window of under-TeV CHAMP abundances.

There is, however, a way to escape all these bounds. A recent paper [12] notes that CHAMPs, if very massive or carrying very small charges. are expelled from the galactic disk by the magnetic fields. That situation prevents any terrestrial or galactic detection and leaves room for CHAMPs to exist. The bound specifically states that particles with  $100(Q/e)^2$  TeV  $\lesssim$  $m \lesssim 10^8 (Q/e)$  TeV are depleted from the disk, and in fact our model (if we forbid the terms in eq. [\(8\)](#page-3-0)) does not fix the hypercharge of E and  $\omega$ , so they an be milli
harged. Unfortunately, this situation is not interesting for our purposes, for this kind of CHAMPs would give rise to very small neutrino magnetic moments and wouldn't show up in the future accelerators, either due to their heavy masses or to their small ouplings.

In conclusion, we need an additional mechanism for E or  $\omega$  decays. The easiest way to accomplish this is by allowing one or more of the couplings in eq.  $(8)$ , which can be taken small, if needed, by arguing that  $(10)$  is an al-most exact symmetry. We discuss one of the possibilities in section [2.3.](#page-6-0) The s
enario of de
aying CHAMPs has, on its own, a number of advantages and drawbacks. Some recent papers  $[13, 14]$  $[13, 14]$  have pointed out that the presence of a massive, harged and olourless parti
le during the pro
ess of primordial nucleosynthesis might lead to an explanation for the cosmic lithium problem. Also, the decay of massive particles during nucleosynthesis could have a dramatic influence in the final abundances of primordial elements, which provides us with bounds on the lifetime and abundan
e of CHAMPs that ould be useful.

# <span id="page-6-0"></span>2.3. Allowing for CHAMP decays

If the particles have to decay the global symmetry [\(10\)](#page-3-1) has to be broken. and for that it is enough to allow some of the terms in eq. [\(8\)](#page-3-0). For the sake of simpli
ity, we will onsider only the ase where the symmetry is softly broken by  $E_L-e_R$  mixing<sup>[2](#page-6-1)</sup>

$$
\mathcal{L}_{\kappa} = \bar{E}_L \kappa e_R + \text{h.c.} \tag{13}
$$

This term will induce decays of  $E$  into SM particles much like the heavy neutrino decays in seesaw models, since only this mixing links the E to the SM degrees of freedom. After diagonalisation of the harged lepton mass matrix one obtains interactions that connect the E to  $W + \nu$ ,  $Z + \ell^{\pm}$  and  $H + \ell^{\pm}$ . As the current bound on heavy charged leptons require that  $m_E > 100 \,\text{GeV}$ , the W and Z will be produ
ed on-shell; the Higgs hannel may or may not be open depending on the actual value of the Higgs and  $E$  masses $^3.$ 

The  $\omega$ , on the other hand, has to decay through the Yukawa  $\bar{E} \nu_R \omega$  vertices; either directly to  $E + \nu_R$  if  $m_\omega > m_E$  or to  $e + \nu_R$  suppressed by the

<span id="page-6-1"></span><sup>2</sup> Sin
e this hoi
e breaks [\(10\)](#page-3-1) softly, none of the other terms in eq. [\(8\)](#page-3-0) need be introdu
ed for the model to remain renormalizable.

<span id="page-6-2"></span><sup>&</sup>lt;sup>3</sup>Note that, as  $U(1)_{\rm em}$  is not broken, flavour-changing vertices involving a photon cannot appear at tree level;  $\Gamma(E \to e\gamma)$  must be at least a one-loop effect, and thereby suppressed.

mixing  $\kappa$ . The simplest situation then arises if  $m_{\omega} > m_E$ , for in that case the  $\omega$ 's will decay into on-shell E's, which in turn will decay in the aforementioned way. In what remains, for simplicity, we shall restrict ourselves to this specific case.

In figure [2](#page-7-0) we present the branching ratios for the decays of the  $E$ . As the de
ays are ontrolled by the would-be Goldstone part of the W and Z (and the Higgs boson if allowed kinemati
ally) they are always proportional to the Yukawa couplings of the charged leptons; therefore, if all the  $\kappa$ 's are of the same order, the  $E$  will decay mainly to the leptons of the third family. We can see that for relatively low masses the dominant channel is  $E \to W \nu_{\tau}$  while for very large masses the ratios tend to the equivalent-Goldstone approximation: 0.5 for the W channel and 0.25 for the  $Z$  and  $H$  channels.



<span id="page-7-0"></span>Figure 2: Dominant decay branching ratios of the vector-like fermion  $E$ . The decays are suppressed by the mass of the charged leptons, thus we have only represented decays into the third family. The Higgs boson mass has been taken to the present best fit,  $m_H = 129 \,\mathrm{GeV}$ .

The decay rates of the E fermion are presented in figure [3](#page-8-1) for  $\kappa_{\tau} = 1 \,\text{GeV}$ . Notice that the rates decrease for large  $m_E$ . This is because the decays proceed through the mixing  $E-\tau$  and this is suppressed by factors  $m_{\tau}/m_E$ ; thus the increase in phase space for large  $m_E$  is compensated by these factors. For the chosen value of  $\kappa_{\tau}$  the decay widths are of the order of the eV. For widths of this order of magnitude the  $E$ 's will not be present at the time

of primordial nucleosynthesis and will not affect it. Note, however, that the decay rates depend on  $\kappa^2_\tau$  $\tau$ , and  $\kappa_{\tau}$  is relatively free, thus the decay rates can vary in several orders of magnitude depending on the value of  $\kappa_{\tau}$ . For  $\kappa_{\tau}$  < 10<sup>-7</sup> GeV the CHAMPs will affect nucleosynthesis and, as commented above, might help to solve the cosmic lithium problem  $[13, 14]$  $[13, 14]$  $[13, 14]$  $[13, 14]$ . We also require  $\kappa_{\tau} > 10^{-16} \text{ GeV}$  to avoid CHAMPs at the present epoch.



<span id="page-8-1"></span>Figure 3: Dominant decay rates of the vector-like fermion  $E$  with the same assumptions made in figure [2.](#page-7-0) For these estimates we have taken  $\kappa_{\tau} = 1 \,\text{GeV}$ .

#### <span id="page-8-0"></span>2.4. Lepton Flavour Violating pro
esses

For general  $\kappa$ 's and Yukawa couplings  $Y_e$ , family lepton flavour is not onserved; one might then worry about possible bounds set by pro
esses like  $\mu \rightarrow 3e$ ,  $\mu \rightarrow e\gamma$  or  $\tau \rightarrow 3\mu$ . We now determine whether the bounds on those rare processes can impose restrictions on the parameters of our model.

The easiest way to calculate the amplitudes for these processes is by using an effective Lagrangian obtained by integration of the  $E$  field. This integration is performed by using the equations of motion for  $E$  and expanding in powers of  $1/m_E$  $1/m_E$  $1/m_E$  (for a detailed example of the integration of a singly charged scalar see  $[15]$ . One then obtains

$$
\mathcal{L}_{\text{LFV}} = -\frac{1}{m_E^4} \overline{e_R} \kappa \kappa^\dagger i \not\!\!D^3 e_R + \cdots \tag{14}
$$

which, after the use of the equations of motion and spontaneous symmetry breaking leads to a lepton flavour violating interaction of the  $Z$  gauge boson with left-handed harged leptons,

<span id="page-9-0"></span>
$$
\mathcal{L}_{LFV} = \frac{e}{2s_W c_W} Z_\mu \overline{e_L} C_{LFV} \gamma^\mu e_L , \qquad C_{LFV} \approx \frac{v^2}{2m_E^4} Y_e \kappa \kappa^\dagger Y_e^\dagger . \tag{15}
$$

 $C_{\text{LFV}}$  is a matrix in flavor space which is not, in general, diagonal; therefore, eq. [\(15\)](#page-9-0) will induce processes such as  $\mu \to 3e$  and  $\tau \to 3\mu$ . Without loss of generality we can take  $Y_e$  diagonal with elements proportional to the charged lepton masses; then we can estimate the branching ratio for the  $\mu \to 3e$ pro
ess as

$$
BR(\mu \to 3e) = \frac{\Gamma(\mu \to 3e)}{\Gamma(\mu \to e\nu\bar{\nu})} \approx \frac{\left|m_e\left(\kappa\kappa^{\dagger}\right)_{e\mu}m_{\mu}\right|^2}{m_E^8}
$$
(16)

Our effective Lagrangian is an expansion in powers of  $1/m_E$  which could be compensated, in part, by  $\kappa \kappa^{\dagger}$  factors in the numerator; thus, for consistency, we should require  $\kappa < m_E$  which allows us to establish an upper bound for the bran
hing ratio. Re
alling also that the present limit on the mass of harged heavy leptons is around 100 GeV, and therefore we should have  $m_E > 100 \,\text{GeV}$ , we obtain

$$
BR(\mu \to 3e) < \left(\frac{m_{\mu}m_{e}}{(100 \,\text{GeV})^2}\right)^2 < 10^{-16} \tag{17}
$$

to be compared with present bounds<sup>[4](#page-9-1)</sup> which are of the order of  $10^{-12}$ . If we apply the same reasoning to  $\tau \to 3\mu$  we see that the branching ratio is enhanced by a  $(m_\tau/m_e)^2$  factor

$$
R(\tau \to 3\mu) \equiv \frac{\Gamma(\tau \to 3\mu)}{\Gamma(\tau \to \mu\nu\bar{\nu})} < \left(\frac{m_{\tau}m_{\mu}}{(100 \,\text{GeV})^2}\right)^2 < 10^{-10} \tag{18}
$$

which is still under the present sensitivity for this ratio, which is about  $10^{-7}$ .

Another very restrictive process is  $\mu \to e\gamma$ , which is bounded at the 10<sup>-11</sup> level,  $BR(\mu \to e\gamma)$  <  $1.2 \times 10^{-11}$ . This limit will be improved in a close future by the MEG experiment by two orders of magnitude  $[17]$ . However,

<span id="page-9-1"></span> $4$ All experimental limits are taken from [16].

this pro
ess an only arise at one loop and it is suppressed by loop fa
tors; therefore, we do not expe
t stringent bounds from it. The ontributions to the oblique parameters are suppressed by powers of the fermions masses and are too small to be observed at the currently available precision.

Finally,  $\mu$ –e conversion in nuclei also provides strong limits in general; for instance,  $\mu$ -e conversion on Ti gives  $\sigma(\mu^-$ Ti  $\rightarrow e^-$ Ti) $/\sigma(\mu^-$ Ti  $\rightarrow$  capture) <  $4.3 \times 10^{-12}$ . In our model, the process is induced by exactly the same interac-tion [\(15\)](#page-9-0) that gives  $\mu \rightarrow 3e$ , and we again do not expect, at present, a strong bound from  $\mu$ –e conversion. However, given the future plans to improve the limits by several orders of magnitude, then perhaps  $\mu$ –e conversion will provide the best bound for LFV processes in this model. In any case, current data on LFV processes cannot constrain this mechanism for E decays.

# <span id="page-10-0"></span>3. The  $\nu_R$  mass and the effective Higgs boson interaction with  $\nu_R$

The model we have discussed contains several sources of lepton number non-conservation: the right-handed neutrino Majorana mass and the h and  $h'$  couplings (if both of them are different from zero). Then it is interesting to ask what is the natural size of the right-handed neutrino Majorana masses. since, even if they are set to zero by hand, radiative corrections involving couplings that do not conserve lepton number will generate them. In fact, by removing the photon line in the diagrams that give rise to the ele
troweak moments, figure [1,](#page-4-0) one obtains a renormalization of the right-handed neutrino Majorana mass. The diagrams are logarithmically divergent and give orre
tions of the type

$$
\delta M_R \sim \frac{h'h}{(4\pi)^2} m_E \tag{19}
$$

(if the scalar  $\omega$  is much heavier than the E, this contribution will have an extra suppression  $(m_E/m_\omega)^2$ ). It is then natural to require  $M_R \gtrsim h' h m_E/(4\pi)^2$ . Of course these type of contributions can be renormalized into  $M_R$  which, after all, is a free parameter of the theory.

In addition, similar diagrams with a vertex  $(\phi^{\dagger} \phi)|\omega|^2$  attached to the  $\omega$ field (see figure [4\)](#page-11-1) give a finite contribution to the  $\left(\phi^\dagger\phi\right)\overline{\nu_R^c}\xi\nu_R$  operator that cannot be avoided. A simple calculation gives

$$
\xi_{ij} = \frac{\lambda_{\omega\phi} f_{\phi}(r)}{(4\pi)^2 4m_E} \left( h_i' h_j^* + h_j' h_i^* \right) \tag{20}
$$



<span id="page-11-1"></span>Figure 4: Diagram contributing to the  $(\phi^{\dagger} \phi) \overline{\nu_R^c} \xi \nu_R$  operator.

where  $f_{\phi}(r)$  can be written in terms of  $f(r)$ , defined in eq. [\(12\)](#page-4-1):  $f_{\phi}(r)$  =  $4f(1/r)/r$ . After spontaneous symmetry breaking this operator gives additional ontributions to the right-handed Ma jorana neutrino mass

$$
\delta M_R \sim \frac{\lambda_{\omega\phi} h' h v^2}{(4\pi)^2 4m_E} \tag{21}
$$

Therefore, at least, one should require

$$
M_R > \frac{\lambda_{\omega\phi} h' h v^2}{(4\pi)^2 4m_E} \sim \frac{\lambda_{\omega\phi} h' h}{(4\pi)^2} 100 \,\text{GeV} \sim 1 \,\text{MeV}
$$
 (22)

where we took  $h' = h = \lambda_{\omega\phi} = 0.1$ . By taking smaller couplings, smaller right-handed neutrino masses would be natural (for instance for  $h' = h =$  $\lambda_{\omega\phi} = 0.01$  one obtains  $M_R > 1 \,\text{keV}$ .

## <span id="page-11-0"></span>4. The Model at olliders

In spite of the fact that the new particles are  $SU(2)$  singlets and only have Yukawa couplings to right-handed neutrinos, they are charged and can be copiously produced at the LHC, if light enough  $(< 1 \text{ TeV})$ , through the Drell-Yan process.

The ross se
tions for proton-proton ollisions an be omputed in terms of the partonic cross sections using the parton distribution functions of the proton (for a very clear review see for instance  $[18]$  $[18]$ ); in figure 5 we present the results<sup>5</sup> for the production total cross sections at the LHC ( $\sqrt{s} = 14 \text{ TeV}$ )

<span id="page-11-2"></span> $5$ We have used the CTEQ6M parton distribution sets [\[19](#page-15-10)]. One could also include next-



<span id="page-12-0"></span>Figure 5: Production cross sections of the charged particles at the LHC ( $\sqrt{s} = 14 \,\text{TeV}$ ) as a function of their masses. m represents either  $m_E$  or  $m_\omega$  depending on the process and X represents that other hadronic or leptonic products are expected in a proton-proton ollision.

as a function of the E and  $\omega$  masses,  $m_E$  and  $m_\omega$  (both represented by m in the figure). Since the particles are produced by  $\gamma$  and Z exchange, there are no unknown free parameters ex
ept the masses of the parti
les. We see that cross sections from 1 fb to 1 pb are easily obtained for the production of  $E$  for masses between 700 GeV and 100 GeV. For the same masses the produ
tion cross section for  $\omega$  is roughly one order of magnitude smaller.

On
e produ
ed in pairs, the parti
les have to be dete
ted and identi fied. The characteristic signatures for this identification are very different depending on the lifetimes of the particles, mostly because if the E and  $\omega$ are long-lived they can be tracked directly in the detectors or, at least, be identified through a displaced decay vertex. The parameter relevant for this behavior is  $\kappa$ , the  $E - e$  mixing.

For  $\kappa \lesssim 1 \,\text{MeV}$ , the E's will have decay lengths roughly over 1 centime-

to-leading-order corrections by multiplying by a  $K$ -factor which typically would change cross sections by  $10-20\%$ . Results have been checked against the CompHEP program [\[20,](#page-15-11)  $21$ .

ter<sup>[6](#page-13-1)</sup>, in fact, for  $\kappa < 0.2 \,\text{MeV}$ , they will go through the detector and behave as a heavy ionizing parti
le. A lot of work has been arried to analyse the signatures of CHAMPs inside the detector (see, for example,  $[22]$ , and  $[23]$  $[23]$ for a re
ent improvement), and also displa
ed verti
es have been dis
ussed (see, for example, [\[24,](#page-15-15) 25]). If  $\kappa > 1$  MeV the E's will decay near the collision point and behave as a fourth generation harged lepton.

Discovering the  $\omega$ 's can be much harder, because they will be produced at a significantly lower rate and the signatures of their decays depend strongly on the details of the model. In the  $m_{\omega} > m_E$  scenario, they will decay quickly into an  $E$  and a heavy neutrino (at least if we want  $h$  and  $h'$  large enough to have significant electroweak moments) and then one has to rely again on the detection of E's unless the heavy neutrino provides a cleaner signal, which is unlikely. In any case, we think that the  $E$ 's, produced in a much greater number, should be onsidered the signature of this model, and perhaps the doorway to understand the  $\omega$  and heavy neutrino decays.

# <span id="page-13-0"></span>5. Con
lusions

We have presented a simple model that generates right-handed neutrino magneti moments and studied its phenomenology. The simplest version of the model ontains CHAMPs (
harged massive stable parti
les) whi
h ould present some problems with standard osmologi
al s
enarios. These problems an easily be evaded by allowing additional ouplings in the Lagrangian. The model can then give rise to various LFV processes at tree level such as  $\mu \rightarrow 3e$ ; however, we have verified that the rates of these processes are strongly suppressed and are well below present and near-future experimental onstraints.

The same interactions that generate the right-handed neutrino magnetic moments will also generate, at one loop, the last operator in eq. [\(1\)](#page-1-2) which provides a lepton number nononserving intera
tion between neutrinos and the SM Higgs boson. This intera
tion gives an additional ontribution to the right-handed neutrino Majorana mass; it is also interesting because could lead to an invisible Higgs decay  $[1]$ . We have computed it and discussed some of its consequences.

<span id="page-13-1"></span> $6$ Note that there's room in the parameter space for this kind of effects even if one requires that CHAMPs do not affect the primordial nucleosynthesis, for if  $\kappa > 100 \text{ eV}$  all the  $E$ 's will have decayed before nucleosynthesis.

Finally, sin
e the parti
les responsible for the right-handed neutrino magneti moment are harged, if light enough they an opiously be produ
ed at the LHC through the Drell-Yan process. We found that the cross sections for Drell-Yan production of E's range from 1 fb to 1 pb for masses between 700 GeV and 100 GeV. For the same range of masses the production cross section for  $\omega$  is roughly one order of magnitude smaller.

In short, we showed that a very simple model giving rise to right-handed neutrino magneti models ompatible with all existing onstraints an easily be constructed. If the right-handed neutrinos are relatively heavy ( $\gtrsim 10 \text{ MeV}$ ) bounds on  $\nu_R$  magnetic moments from red giants or supernovae do not ap $p[y|1]$  and the charged particles responsible for the magnetic moments could be light enough as to be produced and detected at the LHC.

# A
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## Referen
es

- <span id="page-14-0"></span>[1] A. Aparici et al., Phys. Rev. D80 (2009) 013010, 0904.3244.
- <span id="page-14-1"></span>[2] S. Weinberg, Phys. Rev. Lett. 43 (1979) 1566.
- <span id="page-14-2"></span>[3] J. Wudka, J. Phys. G31 (2005) 1401.
- <span id="page-14-3"></span> $|4|$  A. De Rujula, S.L. Glashow and U. Sarid, Nucl. Phys. B333 (1990) 173.
- <span id="page-14-4"></span>[5] S. Dimopoulos et al., Phys. Rev. D41 (1990) 2388.
- <span id="page-14-5"></span>[6] J.L. Basdevant et al., Phys. Lett. B234 (1990) 395.
- <span id="page-14-6"></span>[7] T.K. Hemmick et al., Phys. Rev. D41 (1990) 2074.
- <span id="page-14-7"></span>[8] T. Yamagata, Y. Takamori and H. Utsunomiya, Phys. Rev. D47 (1993) 1231.
- <span id="page-15-0"></span> $[9]$  A. Gould et al., Phys. Lett. B238 (1990) 337.
- <span id="page-15-1"></span>[10] R.S. Chivukula et al., Phys. Rev. Lett.  $65$  (1990) 957.
- <span id="page-15-2"></span>[11] S. Wolfram, Phys. Lett. B82 (1979) 65.
- <span id="page-15-3"></span>[12] L. Chuzhoy and E.W. Kolb, JCAP 0907 (2009) 014, 0809.0436.
- <span id="page-15-4"></span>[13] K. Jedamzik, JCAP 0803 (2008) 008, 0710.5153.
- <span id="page-15-5"></span>[14] K. Jedamzik, Phys. Rev. D77 (2008) 063524, 0707.2070.
- <span id="page-15-6"></span> $[15]$  M.S. Bilenky and A. Santamaria, Nucl. Phys. B420 (1994) 47, [hep-ph/9310302.](http://arxiv.org/abs/hep-ph/9310302)
- <span id="page-15-8"></span>[16] Particle Data Group, C. Amsler et al., Phys. Lett. B667 (2008) 1.
- <span id="page-15-7"></span>[17] MEG, S. Ritt, Nucl. Phys. Proc. Suppl. 162 (2006) 279.
- <span id="page-15-9"></span>[18] J.M. Campbell, J.W. Huston and W.J. Stirling, Rept. Prog. Phys. 70 (2007) 89, [hep-ph/0611148.](http://arxiv.org/abs/hep-ph/0611148)
- <span id="page-15-10"></span>[19] J. Pumplin et al., JHEP 07 (2002) 012, [hep-ph/0201195.](http://arxiv.org/abs/hep-ph/0201195)
- <span id="page-15-11"></span>[20] CompHEP, E. Boos et al., Nucl. Instrum. Meth.  $A534$  (2004) 250, [hep-ph/0403113.](http://arxiv.org/abs/hep-ph/0403113)
- <span id="page-15-12"></span>[21] A. Pukhov et al., CompHEP: A package for evaluation of Feynman diagrams and integration over multi-parti
le phase spa
e. User's manual for version 33, 1999, [hep-ph/9908288,](http://arxiv.org/abs/hep-ph/9908288) INP-MSU-98-41-542. 126pp. User's manual for version 33.
- <span id="page-15-13"></span>[22] M. Fairbairn et al., Phys. Rept. 438 (2007) 1, [hep-ph/0611040.](http://arxiv.org/abs/hep-ph/0611040)
- <span id="page-15-14"></span>[23] J. Chen and T. Adams,  $(2009)$ , 0909.3157.
- <span id="page-15-15"></span>[24] R. Franceschini, T. Hambye and A. Strumia, Phys. Rev. D78 (2008) 033002, 0805.1613.
- <span id="page-15-16"></span>[25] F. de Campos et al., Phys. Rev. D79 (2009) 055008, 0809.0007.