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Measurement of UV-induced absorption and scattering losses in photosensitive fibers

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gratings **UV-assisted** fabrication of using photosensitive fibers is a well-established technique, based on the UV-induced permanent modification of the refractive index of the fiber material. As a result, the absorption coefficient is also changed. Here, we exploit the thermal sensitivity of whispering gallery modes resonances of the fiber itself to measure the profile of the heating along an irradiated fiber versus the input power and for different UV radiation intensities. Our technique allows discriminating between the absorption and scattering contributions to the overall losses, by comparing the results obtained with our technique with direct transmission measurements. Different photosensitive fibers are characterized by means of this technique. Non uniform UV irradiation of photosensitive fibers can be characterized with this technique. © 2018 Optical Society of America

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UV-assisted inscription of fiber Bragg gratings (FBGs) and long period gratings (LPGs) is currently the most employed method for their fabrication. Typically, a photosensitive (PS) fiber is exposed to a UV patterned beam that modulates permanently the refractive index of the core [1]. Some gratings with specific features require of considerable amount of UV energy [2, 3]. The photosensitivity of a given fiber depends on the chemical composition of the core [4, 5]. Here, we will study a germano-silicate boron codoped fiber, a highly germano-silicate doped fiber, and a hydrogenated conventional telecom fiber. According to Kramers-Kronig relations, the change in the refractive index is associated with a variation of the absorption coefficient. Also, the exposure of the fiber to the energy levels of UV-radiation required for gratings inscription may induce a mechanical deformation in the fiber, such as corrugations due to the densification of the material [6] (one should have in mind that for a grating of -30 dB minimum transmittance and 1 cm long, it is needed about 10 minutes of exposure time in order to get a fluence of 150 J/mm²). This leads to the increment of scattering loss of the gratings. A direct transmission measurement during UV-irradiation provides an average of the attenuation coefficient along the total length of the processed section [7], which includes both contributions, i.e., absorption and scattering. Here, we propose to use the whispering gallery mode (WGM) resonances of the fiber itself to measure the increase of the UV-induced absorption loss. Thus combining both types of measurements, one can evaluate the absorption and scattering contributions to the overall losses.

WGM resonances have been demonstrated to be useful for the characterization of optical fibers: thermal effects in active fibers [8], fiber diameter fluctuations [9, 10], and Pockels' coefficients [11]. The WGM resonances are excited azimuthally using an auxiliary microfiber at a given point of the fiber, which plays the role of the microresonator. The optical wavelength of a given resonance is set by the refractive index of the microresonator's material (silica, in our case) and its diameter, which depend on the temperature. The typical high Q-factor of the resonances, between 10^6 and 10^7 , allows achieving very low detection limits (DL) for the temperature variation [8].

First, we will describe the measuring technique. We will use moderate input powers (up to ~ 1 W) in order to induce a measurable temperature variation, ΔT . An increased absorption coefficient will produce a higher heating along the irradiated section, when compared to the pristine fiber section. Moreover, if the section is not uniformly irradiated, it will result in a gradient of temperature along it. The relative wavelength shift of a WGM resonance, $\Delta \lambda / \lambda$, as a function of ΔT is given by:

$$\frac{\Delta\lambda}{\lambda} = \left(\frac{1}{R}\frac{dR}{dT} + \frac{1}{n_{\rm eff}}\frac{dn_{\rm eff}}{dT}\right) \cdot \Delta T \tag{1}$$

where λ is the central wavelength of the unperturbed resonance, R is the fiber radius, and $n_{\rm eff}$ is the effective index of the WGM. The first term of the equation is determined by the material thermal expansion coefficient, and the second depends on both the material thermo-optic effect and the fiber radius thermal expansion. Accurate numerical simulations demonstrate that any WGM resonance centered at 1.55 μ m propagating in a standard optical fiber shifts towards longer wavelengths at the same rate, which was experimentally measured, 8.2 pm/°C [8]. This value is valid for different azimuthal modes and for different radius of the resonator (it changes in less than 0.1% when resonator diameter changes from 100 to 125 μ m). Here we

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will assume that the heating over the transversal section of the fiber, at a given axial position, is determined by the absorption coefficient, α^{abs} [12]. Following the analysis developed in this reference, we find that the steady state value of ΔT , for a given input power P, follows the expression:

$$\frac{\Delta T}{P} = \frac{1}{2\pi bh} \alpha^{\text{abs}}$$
 (2)

where b is the fiber radius and h is the heat transfer coefficient (for standard fiber: $b = 62.5 \ \mu m$ and $h = 81.4 \ W \cdot m^{-2} \cdot K^{-1}$ [12]). Thus, the ratio of ΔT at two different positions along a fiber, 1 and 2, is proportional to the ratio of α^{abs} :

$$\frac{\Delta T_2}{\Delta T_1} = \frac{\alpha_2^{\text{abs}}}{\alpha_1^{\text{abs}}} \tag{3}$$

Figures 1(a) and 1(c) show a scheme of the setup employed for the experiments. WGM resonances are excited at a given point using the evanescent field of a 2 μm auxiliary tapered fiber, placed perpendicularly to the microresonator. The taper can be swept along the fiber to carry out a thermal characterization [13]. This enables a point to point measurement of the temperature profile with a spacial resolution limited by the axial extension of WGM in cylindrical microcavities, which is about 200 μm for a resonance with Q $\sim 10^6$ [14]. A tunable, linearly polarized laser (linewidth < 300 kHz) was launched to the taper through an optical circulator. The setup allows measuring the WGM resonances in transmission (T) and reflection (R) [13]. The polarization controller (PC) included in the setup permits to excite separately the TE and TM resonances. The setup was isolated to prevent external perturbations.

Figure 1(b) shows a typical reflection spectrum of a WGM resonance obtained with our setup ($\lambda_0 = 1540$ nm). The 3-dB spectral linewidth is 36 fm (Q-loaded factor of $4\cdot10^7$). If we assume that the resolution of the technique equals the width of the resonance, then the minimum ΔT that we can measure is $5\cdot10^{-3}$ °C. However, vibrations and other perturbations that are present in our experimental arrangement limit the DL to 0.03 °C.

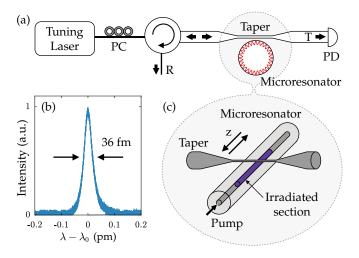


Fig. 1. (a) Scheme of the setup. (b) Reflection trace of a typical WGM resonance. (c) Detail of the relative position between the irradiated fiber and the microtaper.

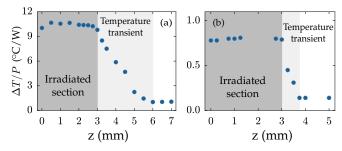


Fig. 2. Typical thermal profile of an irradiated section of PS980. Input signal at (a) 1550 nm, (b) 975 nm.

The thermal profiles of different PS fibers after UV-irradiation were measured. The tested fibers were: (i) Fibercore PS980, $NA \sim 0.13$, cutoff wavelength 940 nm, attenuation 11.4 dB/km at 980 nm; (ii) Fibercore PS1250, NA \sim 0.13, cutoff wavelength 1214 nm, attenuation 131.1 dB/km at 1550 nm; (iii) Fibercore SM1500, NA \sim 0.29, cutoff wavelength 1387 nm, attenuation 1.95 dB/km at 1550 nm; (iv) Corning SMF28, NA \sim 0.14, cutoff wavelength 1260 nm, attenuation 0.188 dB/km at 1550 nm; this fiber was hydrogenated for 15 days (pressure: 30 bar) to increase its photosensitivity. A length of each fiber was exposed to a UV fluence of 150 J/mm², provided by a doubled-argon laser (244 nm). The optical signal launched through them to induce heating was provided by two CW laser sources: (a) an amplified tunable laser (maximum CW power 1 W, tuning range 1530 - 1565 nm, SNR > 50 dB, linewidth < 20 pm), and (b) a monomode fiber-coupled diode laser centered at 975 nm (maximum power 500 mW). During our measurements no significant change of linewidth or line shape was observed, so we concluded that no transverse gradient of temperature was produced.

The thermal profiles of uniformly irradiated sections of different fibers were measured in detail. Figure 2 shows the characterization of fiber PS980 (irradiated section: 5 mm). The UV-fluence used in the irradiation process was 150 J/mm² in a single sweep. Figure 2(a) shows the results when the fiber was illuminated with the 1550 nm optical signal (1 W optical power), while Fig. 2(b) depicts the measurements for the 975 nm laser (500 mW optical power). The results show a clear difference between the irradiated section (z < 3 mm) and the pristine fiber (z > 3 mm). For z > 3 mm, it can be observed a spacial transient governed by the temperature gradient, the heat conduction in silica and the heat transfer to the air. The maximum heating rate obtained when illuminating at 1550 nm is higher than 10 °C/W, while it is lower than 1 °C/W at 975 nm, due to the higher absorption of the irradiated fiber at longer wavelengths. No significant difference in the heating was observed within the range 1530 - 1565 nm.

A direct measurement of transmission loss variation was carried out for fiber PS980, while it was irradiated. First, the loss of the pristine PS980 fiber was measured at 1550 nm by means of the cutback method: a value of 120.0 ± 0.5 dB/km was obtained. Then the UV laser was swept back and forth along a 5 cm section of the fiber, repeatedly (energy delivered: 2.5 J/mm² per swept). The light provided by a LED source (spectral range: 1520-1560 nm) was launched to the fiber, and the output was measured after each swept of the UV laser. The results are shown in Fig. 3(a). The final loss was 6.2 ± 0.4 dB/m (total energy delivered to the fiber: 160 J/mm²). This means that the ratio of

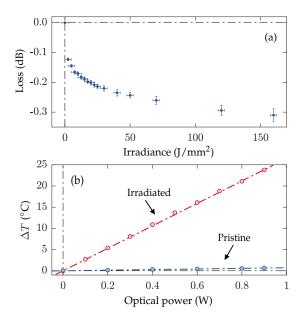


Fig. 3. (a) Direct measurement of the loss as the fiber is irradiated. Length: 5 cm. (b) Thermal heating of the PS980 fiber as a function of the optical power of the input signal (1550 nm).

the attenuation coefficient, α_2/α_1 , was increased in 52 ± 3 times. It should be noted that this attenuation coefficient includes the contribution of absorption and scattering ($\alpha=\alpha^{abs}+\alpha^{scat}$).

The same section of the fiber was used to measure the increase of the absorption coefficient due to the UV illumination, by means of the thermal shift of WGM resonances. The 1550 nm laser signal was launched to the microresonator, and the wavelength shift of the resonances was measured as the power was increased. Results for the temperature variations are shown in Fig. 3(b). The data show a linear trend of the heating with the power of the signal, within and outside of the irradiated section. The temperature of the irradiated section increased at a rate of 26.48 ± 0.15 °C/W, and at 0.718 ± 0.014 °C/W in the pristine fiber. The ratio between both slopes is 36.9 ± 0.7 . Thus, according to Eq. 2, the absorption coefficient is increased in this factor.

The same set of measurements was repeated for fibers PS1250, hydrogenated SMF28, and SM1500, at 1550 nm. The results are compiled in Table 1. It has to be taken into account that,

Table 1. Measurement of thermal heating and loss coefficient of different fibers

	WGM resonances ΔT/P (°C/W)		Direct measurement α (dB/km)	
	Irradiated	Pristine	Irradiated	Pristine
PS980	26.48 ± 0.15	0.718 ± 0.014	6200 ± 400	$120 \pm 2^{(1)}$
PS1250	30.80 ± 0.17	0.768 ± 0.014	6600 ± 400	131.1 ⁽²⁾
H ₂ -SMF28	23.48 ± 0.13	0.815 ± 0.012	5600 ± 400	n/a ⁽³⁾
SM1500	1.20 ± 0.03	< 0.03 ⁽⁴⁾	370 ± 90	1.95 ⁽²⁾

⁽¹⁾ Cutback measurement

Table 2. Comparison between techniques

	WGM resonances	Direct measurement	
	$lpha_2^{ m abs}/lpha_1^{ m abs}$	α_2/α_1	
PS980	36.9 ± 0.7	52 ± 3	
PS1250	40.1 ± 0.8	50 ± 3	
H ₂ -SMF28	28.8 ± 0.5	n/a ⁽¹⁾	
SM1500	$> 40^{(2)}$	190 ± 50	

 $^{^{(1)}}$ Non-available, α_1 unknown

while the WGMs technique allows measuring the absorption coefficient exclusively, the transmission technique also accounts for scattering loss that may happen along the fiber. The comparison between the two techniques is shown in Table 2: the value for $\alpha_2^{abs}/\alpha_1^{abs}$ is obtained from Eq. 3 and the measurements of the heating of the fibers using WGMs, while the ratio α_2/α_1 is calculated from direct transmission measurements of the irradiated fibers.

From these results (Tables 1 and 2), we can stablish some interesting conclusions for the UV effects on the fiber loss. Certainly, the absorption coefficient is substantially increased by a factor between 20 and 40. This is what one could expect and it is consistent with the change of the refractive index that is exploited for the inscription of the fiber gratings. It is worth to point out that the actual values of $\Delta T/P$ demonstrate that in most medium and high power systems the temperature increase will be not negligible. For example, FBGs fabricated with these photosensitive fibers, using a typical value of $\sim 160 \, \text{J/mm}^2$ UV fluence, will exhibit important shifts and chirps [15].

In addition, our results show that the scattering losses are increased even more than the absorption losses. This is the only conclusion compatible with the results summarized in the Table 2, where we see that α_2/α_1 is systematically higher than $\alpha_2^{\text{abs}}/\alpha_1^{\text{abs}}$. If we rewrite α as $\alpha_2^{\text{abs}}+\alpha_1^{\text{scat}}$ and we define r as the ratio between α_2/α_1 and $\alpha_2^{\text{abs}}/\alpha_1^{\text{abs}}$, then we can find the following relationships:

$$\frac{\alpha_2^{\text{abs}}}{\alpha_2} = \frac{\alpha_1^{\text{abs}}}{\alpha_1} \frac{1}{r} \tag{4}$$

$$\frac{\alpha_2^{\text{scat}}}{\alpha_2} = \frac{\alpha_1^{\text{scat}}}{\alpha_1} + \frac{\alpha_1^{\text{abs}}}{\alpha_1} \frac{r - 1}{r}$$
 (5)

Equation 4 shows that when r>1, then the relative contribution of the absorption coefficient decreases after UV radiation, i.e., $\left(\alpha_2^{\rm abs}/\alpha_2\right)<\left(\alpha_1^{\rm abs}/\alpha_1\right)$. Furthermore, Eq. 5 shows that if r>1, then the relative contribution of scattering to the overall loss increase since the last term of the Eq. 5 is positive, i.e., $\left(\alpha_2^{\rm scat}/\alpha_2\right)>\left(\alpha_1^{\rm scat}/\alpha_1\right)$. If we divide Eq. 5 by Eq. 4, then we can show even more clearly how much the relative contribution of scattering is increasing with respect the absorption part for a ratio r>1:

$$\frac{\alpha_2^{\text{scat}}}{\alpha_2^{\text{abs}}} = \frac{\alpha_1^{\text{scat}}}{\alpha_1^{\text{abs}}} \cdot r + (r - 1)$$
 (6)

⁽²⁾ Nominal value

⁽³⁾ Non-available, hydrogenated fiber

 $^{^{(4)}}$ Below detection limit

 $^{^{(2)}}$ ΔT_1 below DL

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Table 3. Absorption and scattering contributions to the overall attenuation coefficient

	α ^{abs} (dB/km)		α ^{scat} (dB/km)	
	Irradiated	Pristine	Irradiated	Pristine
PS980	3680 ± 20	99.7 ± 1.9	2500 ± 400	20 ± 3
PS1250	4280 ± 20	106.6 ± 1.9	2300 ± 400	24.5 ± 1.9
H ₂ -SMF28	3260 ± 18	113.1 ± 1.7	2300 ± 400	n/a ⁽¹⁾
SM1500	167 ± 4	$< 1.95^{(2)}$	200 ± 90	$< 1.95^{(2)}$

⁽¹⁾ Non-available, hydrogenated fiber

The above discussion has been carried out using experimental measurements and Eq. 3. So the conclusions are virtually free of any heat dissipation model, but limited to the evaluation of relative values. However, if we now take into account Eq. 2 and the values of h reported in [12], then we can obtain absolute values for the absorption and scattering contributions to the overall attenuation coefficient. Table 3 summarizes the numerical values that we obtained for α^{abs} using the experimental slopes $\Delta T/P$ and Eq. 2, and the values computed for α^{scat} ($\alpha^{scat} = \alpha - \alpha^{abs}$).

Following this procedure, we are able to provide the two independent contributions α^{abs} and α^{scat} to the overall attenuation coefficient. We can see that in the UV-irradiated fibers both contributions are of the same order of magnitude, even though α^{scat} is smaller, between 0.53 and 0.70 times α^{abs} , excepting fiber SM1500 in which α^{scat} is 1.19 times α^{abs} . In the case of pristine fibers PS980 and PS1250, we can evaluate the two contributions and we see that α^{scat} is between 0.20 and 0.23 times α^{abs} . This confirms that the UV radiation produces an increase of the scattering loss faster than the absorption loss.

The technique based on WGM resonances presents an additional advantage, due to its axial resolution. The direct measurement of the UV-induced loss provides an average result over the length of the section of the fiber under test (in our case, 5 cm), while WGM resonances enables point to point measurements. Thus, it is possible to use this technique in order to study the uniformity of the absorption coefficient (and, hence, both the UV-irradiation and the refractive index variation) along the section of fiber. As a consequence, our technique can be used to detect and correct smooth undesired non-homogeneities or chirps introduced during the fabrication of gratings, taking into

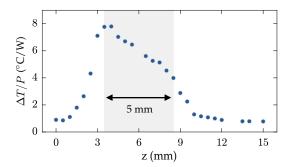


Fig. 4. Thermal profile of an irradiated section of PS980 with a non-uniform UV irradiation along the length of the fiber.

account that the axial resolution of the technique will be larger than the grating period. As a practical example, Fig. 4 shows the thermal profile of a fiber that suffered some misalignment during the UV-irradiation process. The length of the irradiated fiber was 5 mm, and the nominal energy from the UV-laser was 150 J/mm² in a single sweep. The usual input signal (1 W at 1550 nm) was employed. It can be observed that the WGM resonances technique allows identifying and quantifying the different heating along sections of just a few mm, which corresponds to different absorptions coefficients and refractive index increments.

We conclude that the technique presented in this work enables a direct characterization of absorption losses and the uniformity of UV-irradiation in photosensitive fibers. By combining our results with conventional measurements of the fiber attenuation, we can evaluate separately the absorption and scattering contributions to the overall losses. In our experiment, the scattering losses increase faster than the absorption losses under UV-irradiation, although they remain in general lower. We find that our technique might be useful not only for further improvements of photosensitive fibers characteristics, but for the characterization of active and specially doped fibers. For example, it should be possible to study if a specific doping technique increases the scattering losses unnecessarily, but not so much the absorption.

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⁽²⁾ Nominal value

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